## PMP Equations

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## PMP Equations

| No. | Topic | Equation | Equation Explanation | Example Problem with Solution |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Actual Cost (AC) | AC | Actual Cost (AC) represents <br> the total costs actually <br> incurred or spent on a project. <br> It is a direct measure of <br> project expenses. | If the actual cost incurred on a <br> project at a given time is $\$ 15,000$, <br> then AC $=\$ 15,000$. |
| 2 | Planned Value (PV) | PV | Planned Value (PV) represents <br> the authorized budget <br> allocated to the work <br> scheduled to be completed by <br> a specific point in time. | If the planned budget for a <br> project at a given time is $\$ 10,000$, <br> then PV $=\$ 10,000$. |
| 3 | Earned Value (EV) | EV | Earned Value (EV) represents <br> the value of work performed <br> and completed in a project at <br> a specific point in time. | EV = (\% of Work Completed) * <br> Total Budget. <br> In your case, the project actual <br> progress is at $80 \%$, and the total |


|  |  |  |  | $\begin{aligned} & \text { budget is } \$ 1,000,000 \text {. So, to } \\ & \text { calculate } \mathrm{EV}=(80 \%) * \$ 1,000,000, \\ & \mathrm{EV}=0.8 * \$ 1,000,000, \mathrm{EV}= \\ & \$ 800,000 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Cost Variance (CV) | $C V=E V-A C$ | Cost Variance (CV) measures the cost performance by calculating the difference between earned value (EV) and actual cost (AC). | ```If EV =$10,000 and AC = $12,000, then CV = $10,000 - $12,000 = - $2,000.``` |
| 5 | Schedule Variance (SV) | SV = EV - PV | Schedule Variance (SV) assesses the schedule performance by finding the difference between earned value (EV) and planned value (PV). | ```If EV = $8,000 and PV = $10,000, then SV = $8,000 - $10,000 = - $2,000.``` |
| 6 | Earned Value Management (EVM) | $\mathrm{CPI}=\mathrm{EV} / \mathrm{AC}$ | Cost Performance Index (CPI) measures cost efficiency by comparing earned value (EV) to actual cost (AC). | $\begin{aligned} & \text { If } \mathrm{EV}=\$ 800 \text { and } \mathrm{AC}=\$ 1,000, \text { then } \\ & \mathrm{CPI}=\$ 800 / \$ 1,000=0.8 . \\ & \text { (Overbudget) } \end{aligned}$ |
| 7 | Earned Value Management (EVM) | SPI = EV / PV | Schedule Performance Index (SPI) measures schedule efficiency by comparing earned value (EV) to planned value (PV). | $\begin{aligned} & \text { If } \mathrm{EV}=\$ 800 \text { and } \mathrm{PV}=\$ 1,000, \text { then } \\ & \mathrm{SPI}=\$ 800 / \$ 1,000=0.8 . \\ & \text { (Behind schedule) } \end{aligned}$ |
| 8 | Estimate at Completion (EAC)Bad estimation | $\mathrm{EAC}=\mathrm{AC}+\mathrm{ETC}$ | This formula calculates the Estimate at Completion when it's assumed that the current estimation was not accurate and cannot be used for the remaining works. | $\begin{aligned} & \text { If } \mathrm{BAC}=\$ 14,000, \mathrm{AC}=\$ 12,000, \\ & \mathrm{ETC}=\$ 4,000, \text { then } \mathrm{EAC}=\$ 12,000 \\ & +\$ 4,000=\$ 16,000 \end{aligned}$ |
| 9 | Estimate at Completion (EAC) <br> - No Additional Variance - budget rate | $\begin{aligned} & E A C=A C+(B A C- \\ & E V) \end{aligned}$ | This formula calculates the Estimate at Completion when it's assumed that the current variances will continue without any additional variances (parallel to budget). | $\begin{aligned} & \text { If } A C=\$ 12,000, B A C=\$ 20,000, \\ & \text { and } E V=\$ 15,000, \text { then } E A C= \\ & \$ 12,000+(\$ 20,000-\$ 15,000)= \\ & \$ 17,000 . \end{aligned}$ |
| 10 | Estimate at <br> Completion (EAC) <br> - Tough performance | $\mathrm{EAC}=\mathrm{BAC} / \mathrm{CPI}$ | This formula estimates the EAC by assuming that the the project is difficult and performance will remain the same till end. | $\begin{aligned} & \text { If } B A C=\$ 20,000 \text { and } C P I=0.8 \text {, } \\ & \text { then } E A C=\$ 20,000 / 0.8]= \\ & \$ 25,000 \text {. } \end{aligned}$ |
| 11 | Estimate at Completion (EAC) - cost and schedule constraints | $\begin{aligned} & \mathrm{EAC}=\mathrm{AC}+[(\mathrm{BAC} \\ & -\mathrm{EV}) /(\mathrm{CPI} * \mathrm{SPI})] \end{aligned}$ | In this equation, it's assumed that the remaining work will be performed at the cumulative Cost Performance Index CPI, in addition to | $\begin{aligned} & \text { If } \mathrm{AC}=\$ 12,000, \mathrm{BAC}=\$ 20,000 \text {, } \\ & \mathrm{EV}=\$ 15,000, \mathrm{CPI}=1.25 \text {, and SPI } \\ & =0.9, \text { then } \mathrm{EAC}=\$ 12,000+ \\ & {[(\$ 20,000-\$ 15,000) /(1.25 * 0.9)]} \\ & =\$ 19,200 . \end{aligned}$ |


|  |  |  | having schedule or milestone constrains. |  |
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| 12 | To-Complete Performance Index (TCPI) | $\begin{aligned} & \text { TCPI }=(\mathrm{BAC}-\mathrm{EV}) / \\ & (\mathrm{BAC}-\mathrm{AC}) \end{aligned}$ | TCPI predicts the required cost performance to achieve the project's budget at completion (BAC) based on the current performance. TCPI= Remaining Works / Remaining Money | $\begin{aligned} & \text { If } \mathrm{BAC}=\$ 100,000, \mathrm{EV}=\$ 20,000, \\ & \text { and } \mathrm{AC}=\$ 30,000, \text { then TCPI }= \\ & (\$ 100,000-\$ 20,000) /(\$ 100,000- \\ & \$ 30,000)=1.25 . \end{aligned}$ |
| 13 | Three-Point Estimation (Simple Average) | $T E=(O+M+P) / 3$ | Three-Point Estimation calculates the expected duration or cost by averaging optimistic (O), most likely (M), and pessimistic (P) estimates. | If $\mathrm{O}=5$ days, $\mathrm{M}=10$ days, and $\mathrm{P}=$ 20 days, then the Estimation $=(5+$ $10+20$ ) $/ 3=11.6$ days. |
| 14 | Three-Point Estimation (Beta -PERT- Weighted Average) | PERT Estimation = $(O+4 M+P) / 6$ | Program Evaluation and Review Technique (PERT) estimation calculates expected duration using optimistic (O), most likely (M), and pessimistic (P) estimates. | If $\mathrm{O}=5$ days, $\mathrm{M}=10$ days, and $\mathrm{P}=$ 20 days, then PERT Estimation $=(5$ $+4 * 10+20) / 6=10.83$ days. |
| 15 | Float (Total Float and Free Float) | Total Float = LF - EF or LS - ES | Total Float is the amount of time an activity can be delayed without delaying the project's completion date. | If LF $=33$ and $E F=20$, then Total Float $=33-20=13$ days. |
| 16 | Probability and Impact Matrix (Risk Analysis) | Risk Score = <br> Probability * <br> Impact | The Risk Score helps prioritize risks based on their likelihood (Probability) and potential impact (Impact). | If Probability $=0.3$ and Impact $=4$, then Risk Score $=0.3 * 4=1.2$. |
| 17 | Expected Monetary Value (EMV) | EMV = Probability * Impact | EMV is used to calculate the expected financial outcome of a risk by multiplying the Probability by the Impact. | If Probability $=0.4$ and Impact (impact cost in case the risk happened) = $\$ 10,000$, then EMV = 0.4 * \$10,000 = \$4,000. |
| 18 | Communication Channels | $\mathrm{n}(\mathrm{n}-1) / 2$ | This formula calculates the total number of communication channels in a project with n stakeholders. | If there are 5 stakeholders, then the total channels $=5(5-1) / 2=10$ channels. <br> If there are 2 persons added then the total channels $=7(7-1) / 2=21$ channels. <br> And added channel are 2110=11channels. |
| 19 | Present Value (PV) and Future Value (FV) | $P V=F V /(1+r)^{\wedge} n$ | PV calculates the current worth of a future sum of money (FV) considering a discount rate (r) and time ( n ) periods. | $\begin{aligned} & \text { If } \mathrm{FV}=\$ 5,000, r=0.05 \text {, and } \mathrm{n}=3 \\ & \text { years, then } \mathrm{PV}=\$ 5,000 /(1+ \\ & 0.05)^{\wedge} 3=\$ 4,315.46 . \end{aligned}$ |


| 20 | Internal Rate of Return (IRR) | $\begin{aligned} & \text { NPV = } 0=\text { CFO + } \\ & \text { (CF1 / ( } 1+\text { IRR)) }+ \\ & \left(\text { CF2 } /(1+\text { IRR })^{\wedge} 2\right) \\ & +\ldots+(C F n /(1+ \\ & \text { IRR)^n) } \end{aligned}$ | NPV is used to determine the IRR, which is the discount rate at which the net present value (NPV) equals zero. | Solve for IRR when CFO = - $\$ 10,000$, CF1 $=\$ 3,000$, CF2 $=\$ 4,000$, and CF3 $=\$ 5,000$. |
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| 21 | Expected Monetary Value (EMV) for Decision Trees | $\begin{aligned} & \text { EMV = } \\ & \Sigma(\text { Probability * } \\ & \text { Value) } \end{aligned}$ | EMV is used in decision tree analysis to calculate the expected value of various decision alternatives based on probabilities and values. | If Decision A has a Probability of 0.6 and Value of $\$ 10,000$, and Decision $B$ has a Probability of 0.4 and Value of $\$ 8,000$, then EMV $=(0.6$ * $\$ 10,000)+\left(0.4^{*} \$ 8,000\right)=\$ 9,200$. |
| 22 | Present Value of Annuity (PVA) | $\begin{aligned} & \text { PVA }=\text { PMT } *[(1- \\ & \left.\left.(1+r)^{\wedge}-n\right) / r\right] \end{aligned}$ | PVA calculates the present value of a series of equal payments (PMT) made over time, considering a discount rate $(r)$ and the number of periods ( n ). | $\begin{aligned} & \text { If } P M T=\$ 1,000, r=0.06 \text {, and } n=5 \\ & \text { years, then PVA }=\$ 1,000^{*}[(1-(1+ \\ & \left.\left.0.06)^{\wedge}-5\right) / 0.06\right]=\$ 4,212.74 . \end{aligned}$ |
| 23 | Standard Deviation (PERT Analysis) | Standard Deviation $=(P-O) / 6$ | Standard Deviation in PERT analysis estimates the variability in project completion time based on optimistic (O) and pessimistic (P) estimates. | If $\mathrm{O}=10$ days and $\mathrm{P}=20$ days, then Standard Deviation $=(20-10) / 6=$ 1.67 days. |
| 24 | Benefit-Cost Ratio (BCR) | $\begin{aligned} & \text { BCR }=(\mathrm{PV} \text { of } \\ & \text { Benefits) } / \text { (PV of } \\ & \text { Costs) } \end{aligned}$ | $B C R$ evaluates the profitability of an investment by comparing the present value of benefits to the present value of costs. | ```If PV of Benefits = $40,000 and PV of Costs = $30,000, then BCR = $40,000 / $30,000 = 1.33.``` |
| 25 | Return on Investment (ROI) | $\begin{aligned} & \hline \text { ROI = (Net Profit / } \\ & \text { Investment) * } 100 \end{aligned}$ | ROI measures the profitability of an investment by calculating the percentage return relative to the initial investment. | ```If Net Profit = $20,000 and Investment = $50,000, then ROI = ($20,000 / $50,000) * 100 = 40%.``` |
| 26 | Work Performance Data (WPD) | WPD = Output from Executing a Process | WPD includes data on project work performance collected during the execution of project activities. | Examples of WPD include completed deliverables, test results, and issue logs. |
| 27 | Net Present Value (NPV) | $\begin{aligned} & \text { NPV }=\sum(\text { Cash Flows } \\ & \left./(1+r)^{\wedge} n\right) \end{aligned}$ | NPV evaluates the attractiveness of an investment by summing the present values of expected cash flows over time, considering a discount rate $(r)$ and periods ( $n$ ). | If cash flows for five years are $\$ 5,000, \$ 1,000, \$ 2,000, \$ 2,500$, and $\$ 3,000$ with a discount rate of $0.1(10 \%)$, then NPV $=-\$ 5,000 /(1+$ $0.1)^{\wedge} 1+\$ 1,000 /(1+0.1)^{\wedge} 2+$ $\$ 2,000 /(1+0.1)^{\wedge} 3+\$ 2,500 /(1+$ $0.1)^{\wedge} 4+\$ 3,000 /(1+0.1)^{\wedge} 5=$ \$314.88. |
| 28 | Cost Performance Index (CPI) | CPI = EV / AC | Cost Performance Index (CPI) measures cost efficiency by calculating the ratio of earned value (EV) to actual cost (AC). | $\begin{aligned} & \text { If } \mathrm{EV}=\$ 15,000 \text { and } \mathrm{AC}=\$ 12,000, \\ & \text { then } \mathrm{CPI}=\$ 15,000 / \$ 12,000= \\ & 1.25 . \end{aligned}$ |


| 29 | Schedule <br> Performance Index <br> (SPI) | SPI = EV / PV | Schedule Performance Index <br> (SPI) assesses schedule <br> efficiency by finding the ratio of <br> earned value (EV) to planned <br> value (PV). | If EV = \$9,000 and PV = \$10,000, <br> then $\mathrm{SPI}=\$ 9,000 / \$ 10,000=0.9$. |
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| 30 | Payback Period | Payback Period $=$ <br> Initial Investment / <br> Annual Cash Flow | Payback Period calculates the <br> time required to recover the <br> initial investment based on <br> annual cash flows. | If the initial investment is \$50,000, <br> and the annual cash flow is <br> $\$ 20,000$, then the Payback Period $=$ <br> $\$ 50,000 / \$ 20,000=2.5$ years. |

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